10.5 Videos Guide

10.5a

- Equations of conic sections
 - o Circle

$$(x-h)^2 + (y-k)^2 = r^2$$

- o Parabolas
 - Horizontally oriented axis of symmetry
 - $y^2 = 4px$

•
$$(y-k)^2 = 4p(x-h)$$

- Vertically oriented axis of symmetry
 - $x^2 = 4py$

•
$$(x-h)^2 = 4p(y-k)$$

10.5b

Introduction to the ellipse

10.5c

- Equations and properties of ellipses
 - Ellipses
 - Horizontally oriented major axis

•
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

• $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$

Vertically oriented major axis
$$\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$$

$$\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1$$

- Note that a > b
- Locations of foci are given by $a^2 = b^2 + c^2$
- Eccentricity is $e = \frac{c}{a}$ (more circular if e is close to 0 and more elongated if e is close to 1)

10.5d

- Hyperbolas
 - o Horizontally oriented transverse axis

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$

o Vertically oriented transverse axis

$$\frac{y^2}{b^2} - \frac{x^2}{a^2} = 1$$

$$\frac{(y-k)^2}{b^2} + \frac{(x-h)^2}{a^2} = 1$$
O Location of foci are given by $c^2 = a^2 + b^2$

10.5e

• Asymptotes of a hyperbola: $y - k = \pm \frac{b}{a}(x - h)$